

# Carmela Marangi

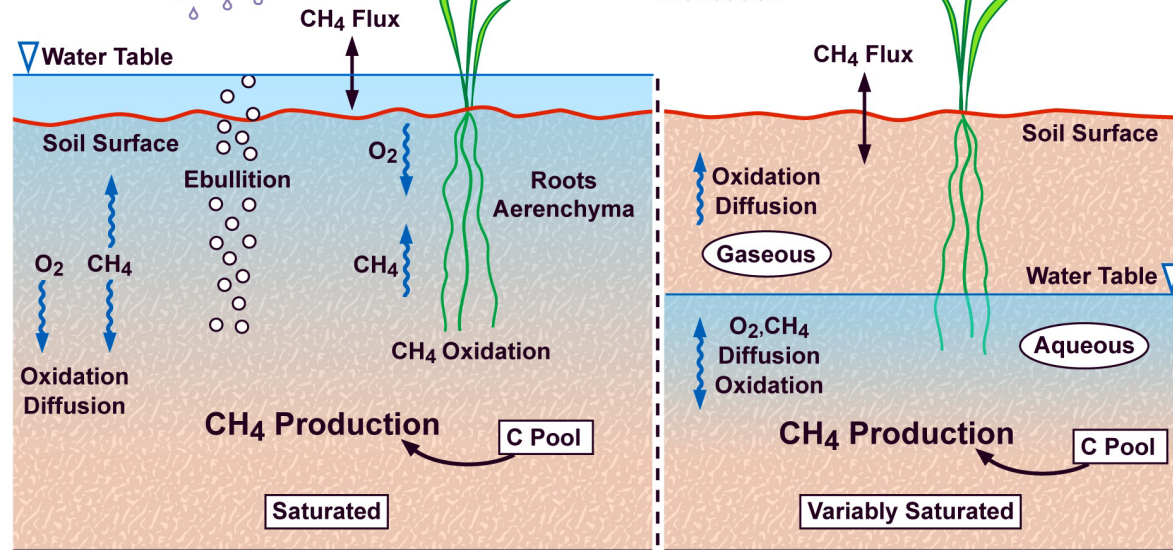
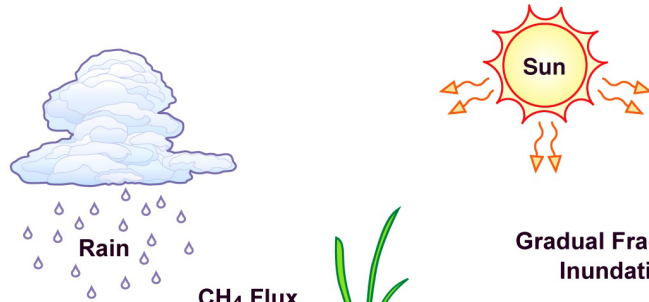
*Modelling of Soil Organic Carbon dynamics in wetlands*



*Joint work of V. Bohaienko, F. Diele, C. Marangi, A. Martiradonna, A. Provenzale*



# Modelling of Soil Organic Carbon Dynamics in Wetlands

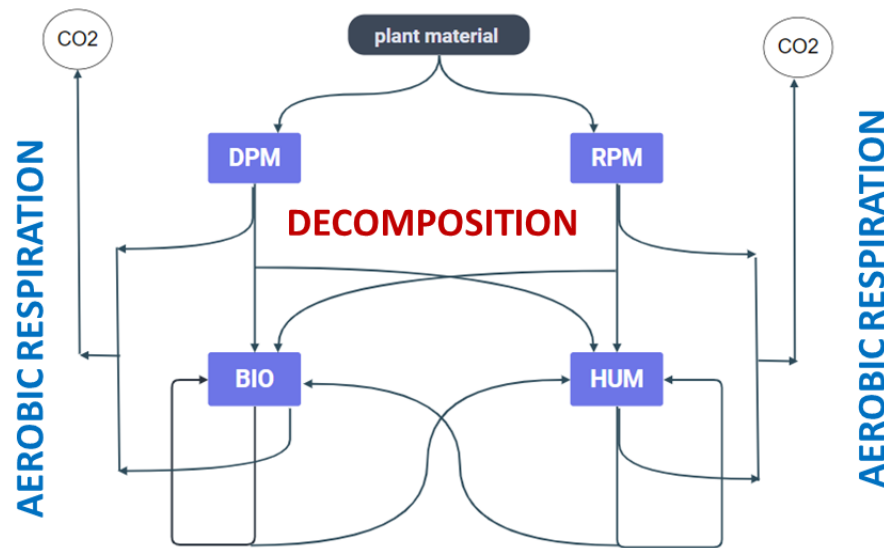


Riley, W. J., Subin, Z. M., Lawrence, D. M., Swenson, S. C., Torn, M. S., Meng, L., ... & Hess, P. (2011). Barriers to predicting changes in global terrestrial methane fluxes: analyses using CLM4Me, a methane biogeochemistry model integrated in CESM. *Biogeosciences*, 8(7), 1925-1953.



## Model's assumption:

In unsaturated zones of soil SOC decomposition is performed by bacteria that respire  $\text{CO}_2$

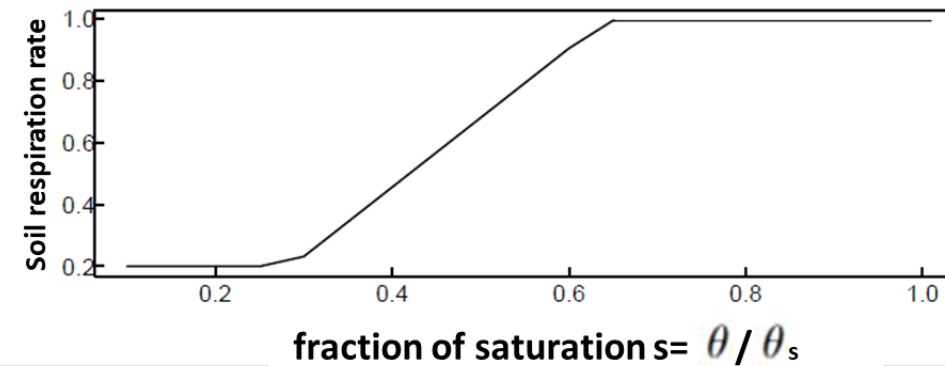


Diele, F., Marangi, C., & Martiradonna, A. (2021). Non-standard discrete RothC models for soil carbon dynamics. *Axioms*, 10(2), 56.

## Carbon decomposition is modeled by:

Intrinsic respiration rates that describe the transition from bacteria activity resulting in  $\text{CO}_2$  generation

## Modifying rate factor for soil moisture

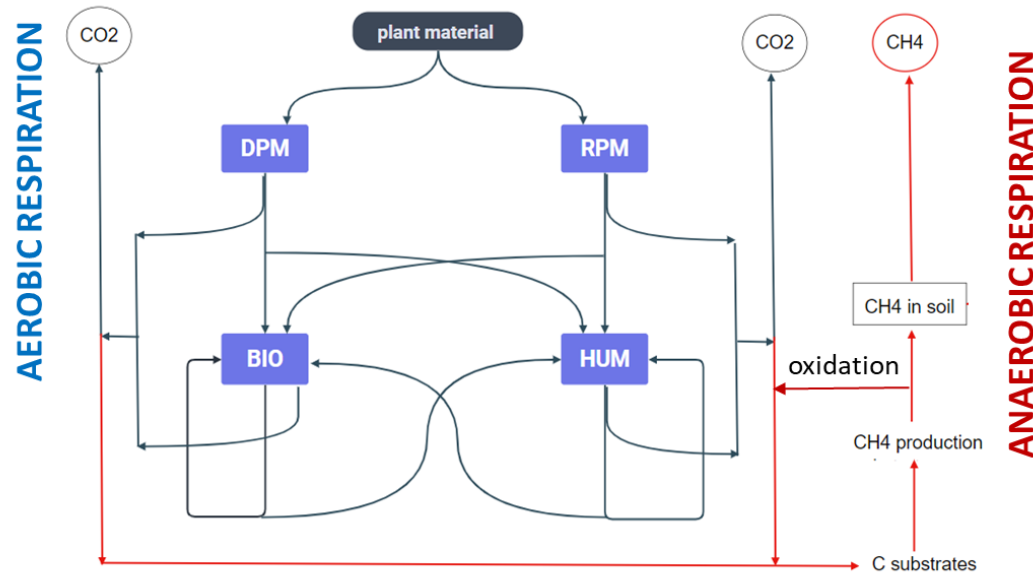


# Model's assumptions

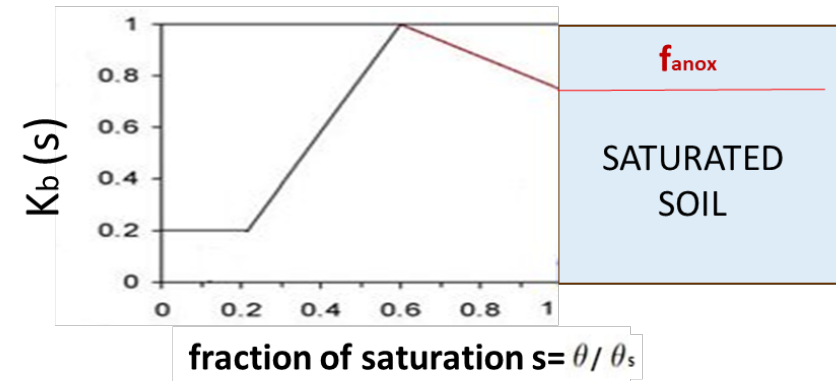


## Model's assumption:

In large saturated zones of soil SOC decomposition is performed by different bacteria that respire  $\text{CO}_2$  or  $\text{CH}_4$



Zhang, Y., Li, C., Trettin, C. C., Li, H., & Sun, G. (2002). An integrated model of soil, hydrology, and vegetation for carbon dynamics in wetland ecosystems. *Global biogeochemical cycles*, 16(4), 9-1.



## Modifying rate factor for soil moisture

$$K_b(s) = \begin{cases} 0.2, & \text{if } s(t) \leq s_{min} \\ 1 - 0.8 \frac{s_0 - s(t)}{s_0 - s_{min}}, & \text{if } s_{min} < s(t) \leq s_0 \\ 1 - (1 - f_{anox}) \frac{s(t) - s_0}{1 - s_0}, & \text{if } s_0 < s(t) \leq 1 \end{cases}$$

# In-depth RothC for wetlands



The vertical water flow can be significant in wetlands and can influence the dynamics of in-depth SOC concentration

## Model's structure

- Water head pressure  $h=h(z,t)$  [L] dynamics in saturated/unsaturated soil described by **Richardson equation** (1D Richards' equation)
- **SOC diffusion-advection-reaction equations** were:
  - reaction given by **modified RothC for wetland** (described before);
  - advection term  $v(z,t) = K(h) \left( \frac{\partial h}{\partial z} - 1 \right) [LT^{-1}]$  for describing the transport of SOC due to vertical water flow related to  $h$  according to the Darcy's law
- **temperature transport equation** for describing the dynamics of in-depth temperature distribution

water table

$h(z,t) < 0$

$h(z,t) > 0$

$z=0$

Saturated soil

$z=L$



# In-depth RothC for wetlands

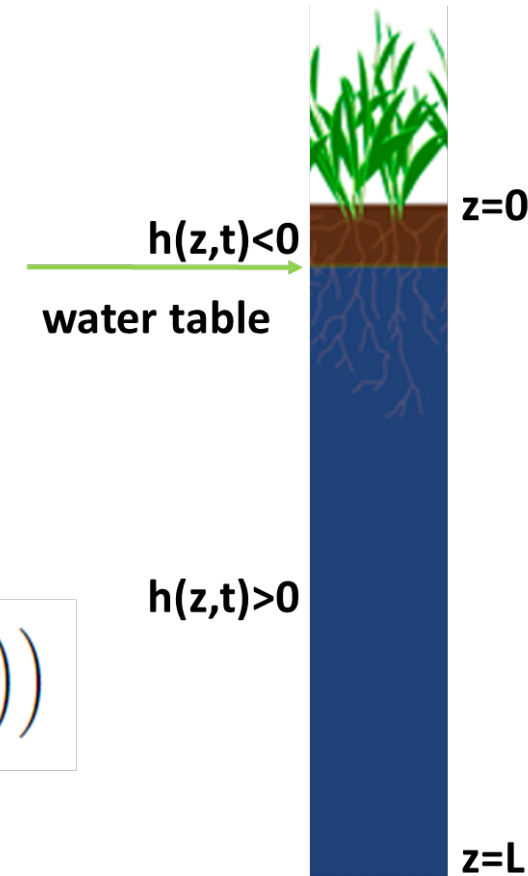


The vertical water flow can be significant in wetlands and can influence the dynamics of in-depth SOC concentration

## Model's structure

- Water head pressure  $h=h(z,t)$  [L] dynamics  
Richardson equation (1D Richards' equation)

$$\left( C(h, z) + \frac{\theta(h, z)}{\theta_s(z)} S_s(z) \right) \frac{\partial h(z, t)}{\partial t} = \frac{\partial}{\partial z} \left( k(h, z) \left( \frac{\partial h(z, t)}{\partial z} - 1 \right) \right)$$



# In-depth RothC for wetlands



The vertical water flow can be significant in wetlands and can influence the dynamics of in-depth SOC concentration

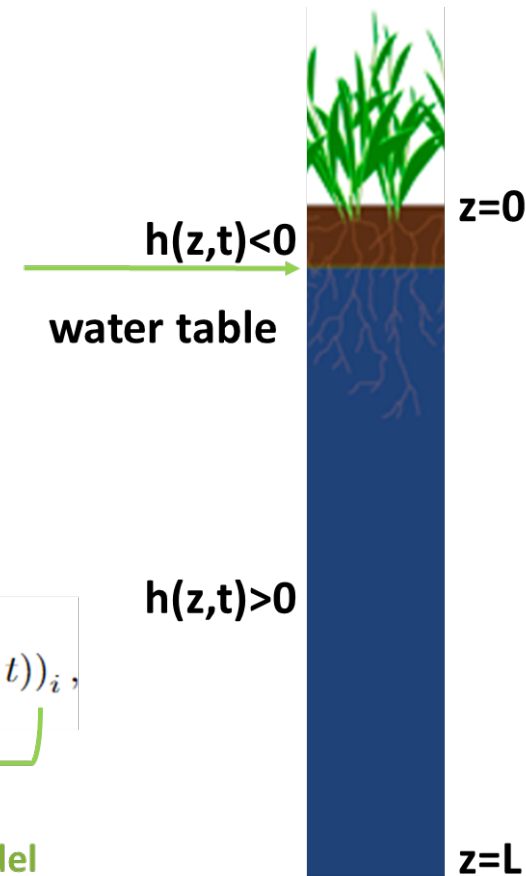
## Model's structure

- SOC compounds diffusion-advection-reaction equations, the reaction part of which is in the form of RothC model for wetland;

$$\sigma \frac{\partial c_i(z, t)}{\partial t} = D_i \frac{\partial^2 c_i(z, t)}{\partial z^2} - v(z, t) \frac{\partial c_i(z, t)}{\partial z} + \underbrace{(\rho(z, t) A c(z, t) + b(z, t))}_i,$$

$$i = 0, \dots, 3$$

Original RothC model



# In-depth RothC for wetlands



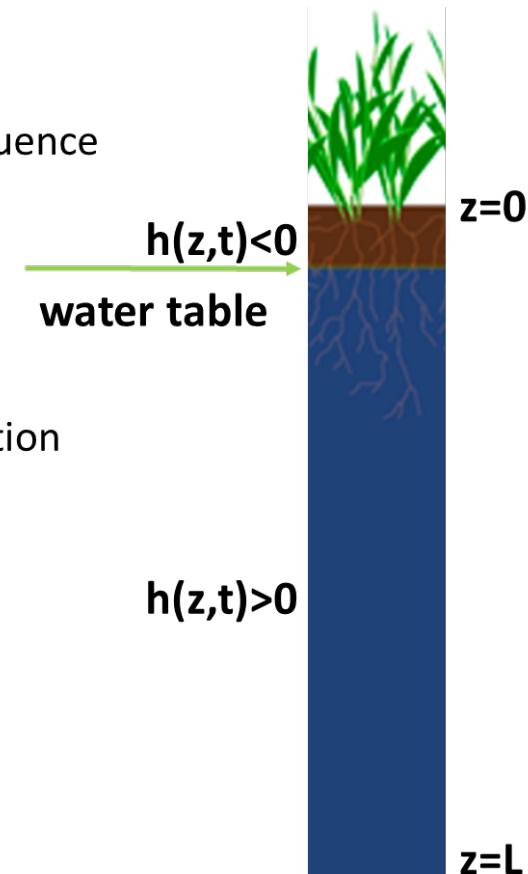
The vertical water flow can be significant in wetlands and can influence the dynamics of in-depth SOC concentration

## Model's structure

- Temperature transport equation (to consider in depth distribution of temperature influence of microbial activity).

$$C_T \frac{\partial T}{\partial t} = \frac{\partial}{\partial z} \left( \lambda \frac{\partial T}{\partial z} \right) - v(z) \frac{\partial T}{\partial z}$$

$$T|_{z=0} = T_a, \quad \frac{\partial T}{\partial z} \Big|_{z=L} = 0$$





# Boundary conditions



In-depth RothC for wetlands.

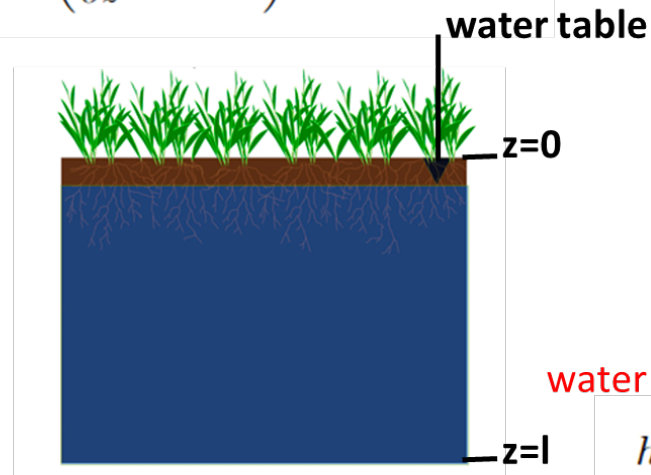
**Boundary conditions that can take into account periodical flooding**

$h(z,t)$ : water head pressure

**Non submerged soil:**

prescribed flow (Neumann condition)

$$-K(h(0,t)) \left( \frac{\partial h}{\partial z}(0,t) - 1 \right) = P(t) - E(t)$$



$$l_e(t)$$

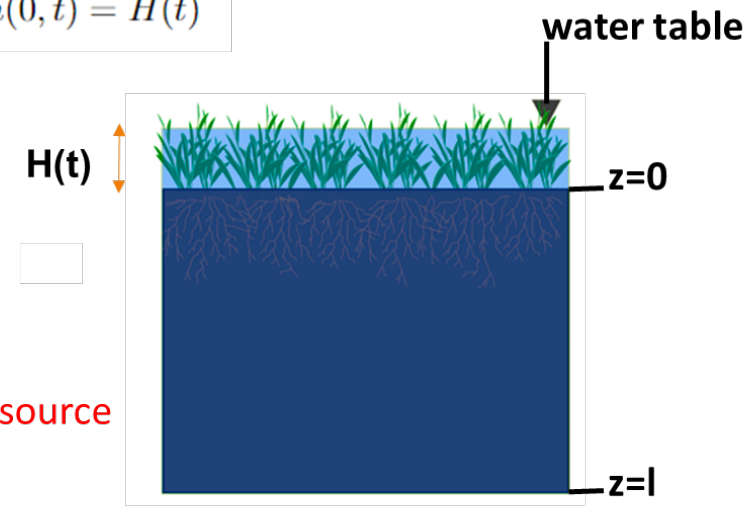
water level in an external source

$$h(l,t) = l - l_e(t)$$

**Submerged soil:**

prescribed value (Dirichlet condition)

$$h(0,t) = H(t)$$





*The considered scenario was the growth of rice in the lands of Ebro Delta. Rice fields are flooded from the end of April to September-October. Flooding was modelled by linear change of water level  $Le(t)$  from the value below bottom depth in December-January to the level of 10 cm above soil surface in May-September*

*Monthly averaged precipitation and air temperature data was taken from the website <https://en.climate-data.org/europe/spain/catalonia/amposta-56879/> for the city of Amposta, the nearest to the Ebro delta. Having only temperature data, evapotranspiration was calculated according to the Hargreaves-Saman formula*

*M. Belenguer-Manzanedo, C. Alcaraz, M. Martinez-Eixarch, A. Camacho, J. Morris, C. Ibanez, Modeling soil accretion and carbon accumulation in deltaic rice fields, Ecological Modelling 484 (2023) 110455*



| Param.     | Description                     | Value                    | Dimension | Ref.  |
|------------|---------------------------------|--------------------------|-----------|---|
| $\theta_r$ | Residual water content          | 0.098                    | $m/day$   | Obtained from clay, silt, and sand content using Rosetta v.1 model        |
| $\theta_s$ | Saturated water content         | 0.422                    |           | -//-  |
| $a$        | van Genuchten model's parameter | 0.005                    |           | -//-  |
| $n$        | -//-                            | 1.436                    |           | -//-  |
| $K_s$      | Coefficient of filtration       | $1.18 \cdot 10^{-2}$     |           | -//-  |
| $\beta$    | Mualem model's parameter        | 0.678                    | $m^{-1}$  | -//-  |
| $S_s$      | Specific storage                | $10^{-5}$ –<br>$10^{-3}$ |           | Possible range of values for silt-rich soils according to the data in [5] |
| $l$        | Bottom depth                    | 1                        | $m$       | [6]   |

Table 1: The values of parameters for the Richards’ - Richardson equation

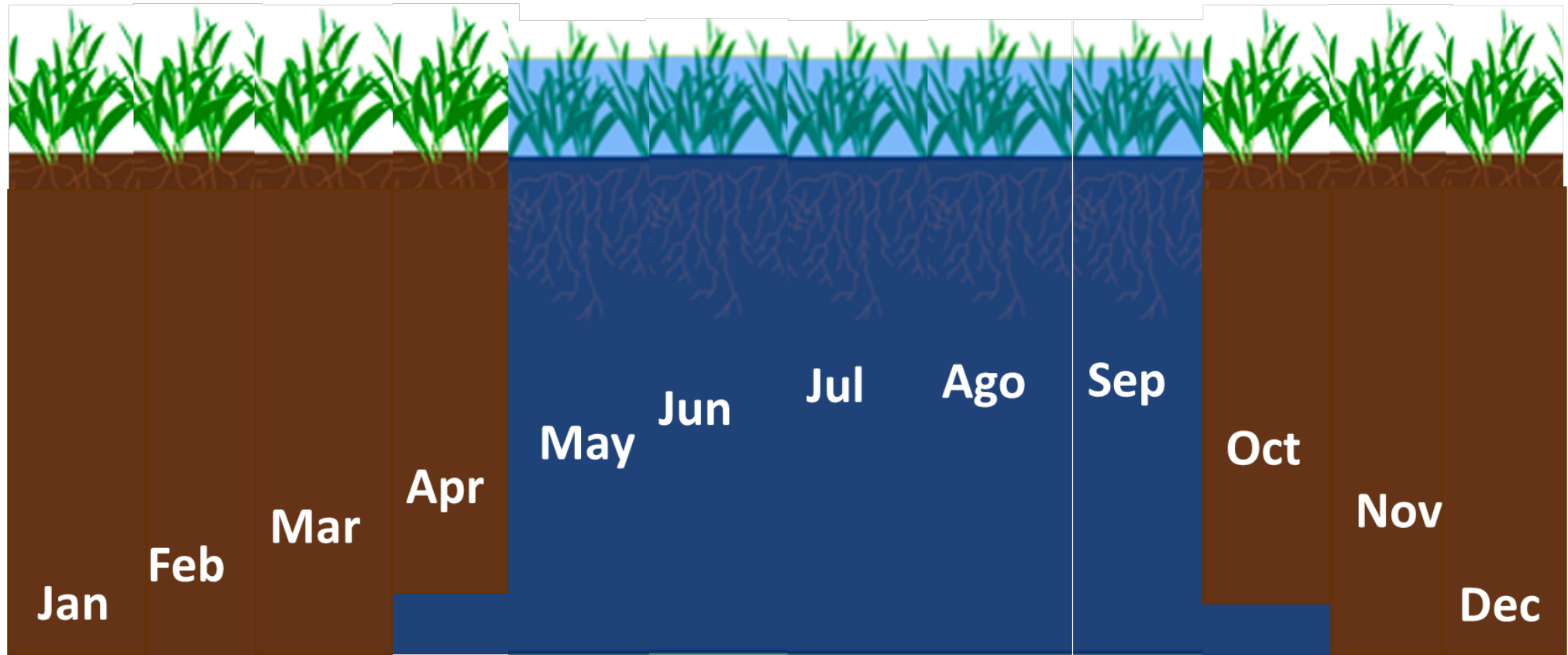
| Month | ET,<br><i>mm/day</i> | Precipitation,<br><i>mm/day</i> | $L_e, m$ |
|-------|----------------------|---------------------------------|----------|
| Jan   | 0.95                 | 1.47                            | 4        |
| Feb   | 1.21                 | 1.12                            | 2.5      |
| Mar   | 1.81                 | 1.38                            | 1.5      |
| Apr   | 2.59                 | 1.81                            | 0.75     |
| May   | 3.37                 | 1.90                            | -0.1     |
| Jun   | 4.23                 | 0.95                            | -0.1     |
| Jul   | 4.41                 | 0.77                            | -0.1     |
| Aug   | 4.15                 | 1.21                            | -0.1     |
| Sep   | 3.28                 | 2.33                            | -0.1     |
| Oct   | 2.33                 | 2.51                            | 0.75     |
| Nov   | 1.38                 | 1.73                            | 2.5      |
| Dec   | 0.95                 | 1.47                            | 4        |

Table 2: The values of parameters





## One-year simulation



# References



Bohaienko, V.; Diele, F.; Marangi, C.; Tamborrino, C.; Aleksandrowicz, S.; Woźniak, E. A Novel Fractional-Order RothC Model. *Mathematics* 2023, 11, 1677. <https://doi.org/10.3390/math11071677>

Diele F., Luiso I., Marangi C., Martiradonna A., SOC-reactivity analysis for a newly defined class of two-dimensional soil organic carbon dynamics, *Applied Mathematical Modelling*, Volume 118, 2023, Pages 1-21, <https://doi.org/10.1016/j.apm.2023.01.015>.

Diele, F., Luiso, I., Marangi, C. et al. Evaluating the impact of increasing temperatures on changes in Soil Organic Carbon stocks: sensitivity analysis and non-standard discrete approximation. *Comput Geosci* 26, 1345–1366 (2022), <https://doi.org/10.1007/s10596-022-10165-3>.

Diele, F., Marangi, C., Martiradonna, A. (2021). *Non-Standard Discrete RothC Models for Soil Carbon Dynamics*, *Axioms*, 10(2), 56.

<https://github.com/CnrlacBaGit/NSRothC>

# LifeWatch ERIC 2024 Thematic Service Workshop Series

Thank you for your attention!  
**Any questions?**



**Taxonomy** | Brussels, Belgium, 30 January 2024



**Climate Change Impact on Biodiversity Patterns** | Lecce, Italy, 21-22 February 2024



**Animal Movement and Biologging** | Ostend, Belgium, 22 March 2024



**Biogeography** | Bologna, Italy, 4-5 April 2024



**Biodiversity Observatory Automation** | Ljubljana, Slovenia, 11 April 2024



**Habitat Mapping** | Aveiro, Portugal, 3 May 2024

